

```

> restart;
> with(LinearAlgebra):
> M:=Matrix([[ xA , yA , xA^2+yA^2 , 1 ],
              [ xB , yB , xB^2+yB^2 , 1 ],
              [ xC , yC , xC^2+yC^2 , 1 ],
              [ xD , yD , xD^2+yD^2 , 1 ]]);

```

$$M := \begin{bmatrix} xA & yA & xA^2 + yA^2 & 1 \\ xB & yB & xB^2 + yB^2 & 1 \\ xC & yC & xC^2 + yC^2 & 1 \\ xD & yD & xD^2 + yD^2 & 1 \end{bmatrix} \quad (1)$$

```

> W:=Matrix([[ xA , yA , 1 ],
              [ xB , yB , 1 ],
              [ xC , yC , 1 ]]);

```

$$W := \begin{bmatrix} xA & yA & 1 \\ xB & yB & 1 \\ xC & yC & 1 \end{bmatrix} \quad (2)$$

```

> Determinant(W);

```

$$xAyB - xAyC - xByA + xByC + xCyA - xCyB \quad (3)$$

```

> Determinant(M);

```

$$\begin{aligned}
& xA^2 xB yC - xA^2 xB yD - xA^2 xC yB + xA^2 xC yD + xA^2 xD yB - xA^2 xD yC - xA xB^2 yC \\
& + xA xB^2 yD + xA xC^2 yB - xA xC^2 yD - xA xD^2 yB + xA xD^2 yC - xA yB^2 yC + xA yB^2 yD \\
& + xA yB yC^2 - xA yB yD^2 - xA yC^2 yD + xA yC yD^2 + xB^2 xC yA - xB^2 xC yD - xB^2 xD yA \\
& + xB^2 xD yC - xB xC^2 yA + xB xC^2 yD + xB xD^2 yA - xB xD^2 yC + xB yA^2 yC - xB yA^2 yD \\
& - xB yA yC^2 + xB yA yD^2 + xB yC^2 yD - xB yC yD^2 + xC^2 xD yA - xC^2 xD yB - xC xD^2 yA \\
& + xC xD^2 yB - xC yA^2 yB + xC yA^2 yD + xC yA yB^2 - xC yA yD^2 - xC yB^2 yD + xC yB yD^2 \\
& + xD yA^2 yB - xD yA^2 yC - xD yA yB^2 + xD yA yC^2 + xD yB^2 yC - xD yB yC^2
\end{aligned} \quad (4)$$