

# Thermodynamics of cationic and anionic surfactant interaction

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October 7, 2013



# Introduction

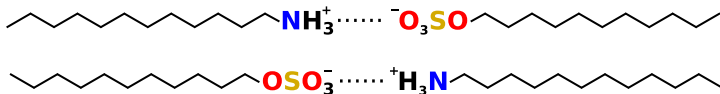
## Motivation

- Fundamental understanding of hydrophobic and ionic forces in lipid membranes and proteins
- Simple model system is the interacting positively and negatively charged linear surfactants
- Dissection of the hydrophobic and ionic contributions to the thermodynamics of surfactant interactions

# Introduction

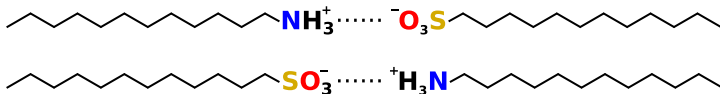
Model system / objects of investigation

Alkylamine interactions with alkyl sulfates



and

alkylamine interactions with alkane sulfonates



# Model

## Reaction between oppositely charged detergents

Reaction between negatively and positively charged detergents can be divided into two arbitrary parts:

- 1 oppositely charged ions form ion pairs



and

- 2 electrically neutral and hydrophobic ion pair complexes form an aggregate of size  $\nu$



which precipitates out of aqueous solution.

$R_1$  and  $R_2$  are linear aliphatic chains of various length.

# Isothermal titration calorimetry

Thermogram and binding isotherm of decane sulfonate titration by dodecylammonium

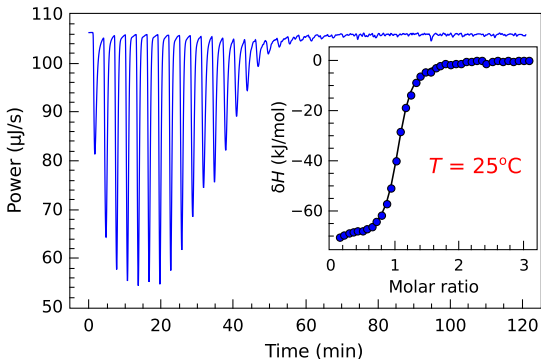
## Equipment:

Microcal (Northampton, MA)  
Micro Calorimetry System  
(MCS)

Temperature range:  
(25–65) °C

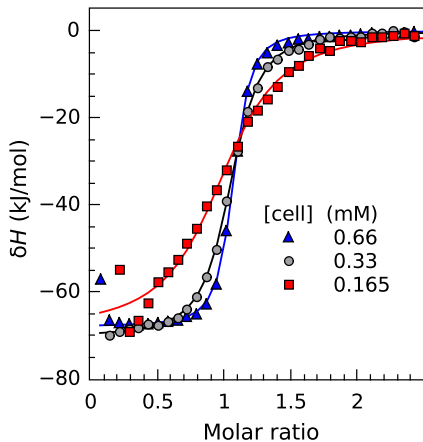
## Surfactant concentrations:

Cell – 0.33 mM  
Syringe – 5 mM



# Observed binding constant dependence on concentration

Example: dodecylammonium binding to decane sulfonate at  $T = 25\text{ }^\circ\text{C}$

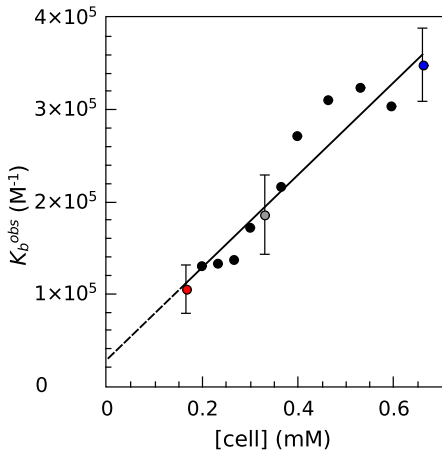
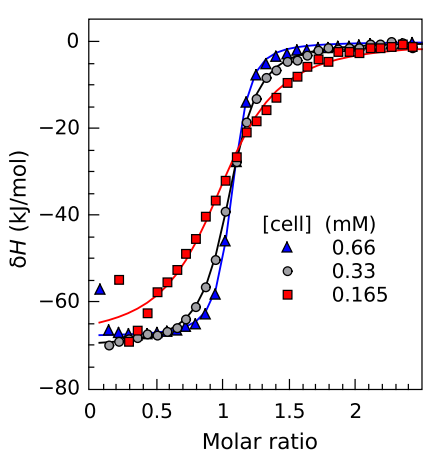


$C$ (mM)	$K_b^{obs}$ ( $M^{-1}$ )	$K_b^{mod}$ ( $M^{-1}$ )
0.66	$3.5 \times 10^5$	$5.5 \times 10^5$
0.33	$1.9 \times 10^5$	$2.7 \times 10^5$
0.165	$1.1 \times 10^5$	$1.4 \times 10^5$

$$K_b^{mod} = \frac{[R_1NH_3^+ \cdots R_2SO_3^- \downarrow]}{[R_1NH_3^+][R_2SO_3^-]}$$

# Observed binding constant dependence on concentration

Example: dodecylammonium binding to decane sulfonate at  $T = 25\text{ }^{\circ}\text{C}$

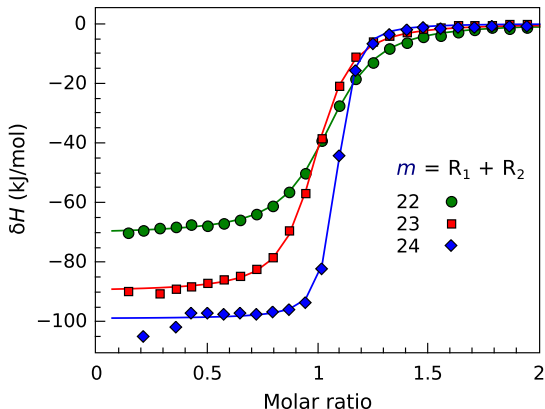


# Dependence on aliphatic chain length

Example: dodecylammonium binding to alkane sulfonate

Number of carbon atoms in both  $R_1$  and  $R_2$  linear aliphatic chains:

$$m = R_1 + R_2$$





# Dependence on aliphatic chain length

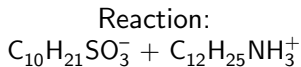
Alkane sulfonate binding to alkylammonium at 25°C

**Table:** Thermodynamic parameters of stoichiometric coprecipitate formation. Gray columns mark experimentally obtained values.

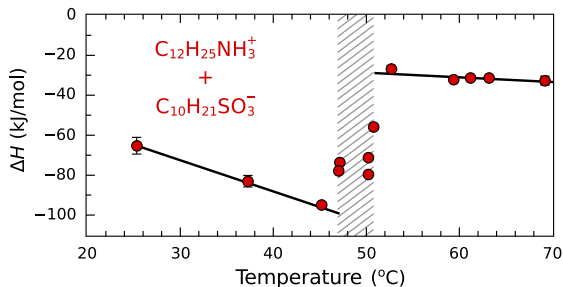
<i>m</i>	$K_b^{obs}$ (M <sup>-1</sup> )	$K_b^{mod}$ (M <sup>-1</sup> )	$\Delta_{agg}G$ (kJ/mol)			$\Delta_{agg}H$ (kJ/mol)		
			<i>obs</i>	<i>mod</i>	<i>alk</i>	<i>obs</i>	<i>mod</i>	<i>alk</i>
21	3.3 × 10 <sup>4</sup>	6.4 × 10 <sup>4</sup>	-25.8	-27.5	-56.0	-37.4	-97.4	-90.8
22	1.8 × 10 <sup>5</sup>	2.7 × 10 <sup>5</sup>	-30.0	-31.0	-59.6	-67.5	-102.6	-96.0
23	2.6 × 10 <sup>5</sup>	1.2 × 10 <sup>6</sup>	-30.9	-34.6	-63.2	-81.9	-107.8	-101.2
24	1.3 × 10 <sup>6</sup>	4.9 × 10 <sup>6</sup>	-34.9	-38.2	-66.8	-91.1	-113.0	-106.4

# Enthalpy dependence on temperature

Example: decane sulfonate reaction with dodecylammonium



Solid-to-liquid phase  
transition at 49°C



# Enthalpy dependence on temperature

Example: decane sulfonate reaction with dodecylammonium

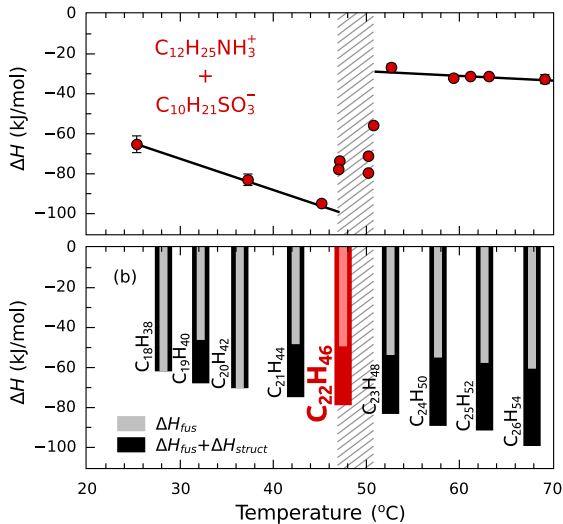
Reaction:



Solid-to-liquid phase transition at 49°C

Alkanes:

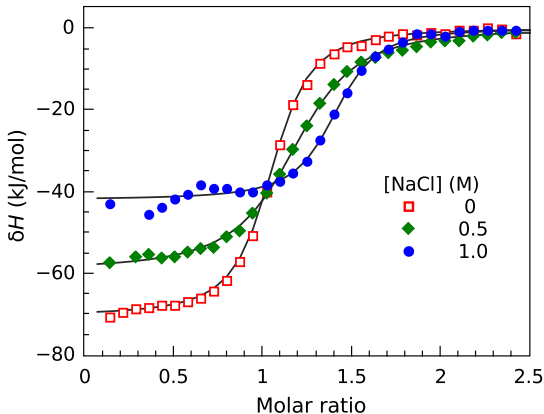
Data taken from CRC Handbook\*



\* CRC Handbook of Chemistry and Physics, 90th ed.; CRC Press: Boca Raton, FL, 2009

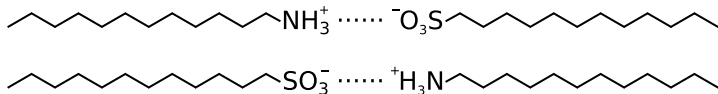
# Enthalpy dependence on salt concentration

Dodecylammonium binding to alkane sulfonate at various salt concentrations



# Dissection of thermodynamic aggregation parameters

Hydrophobic and ionic contributions of dodecylamine binding to dodecane sulfonate



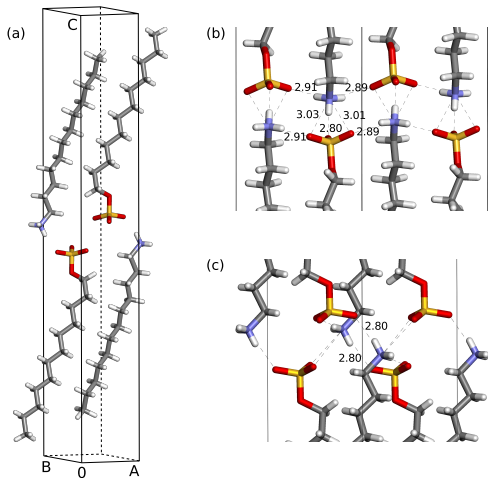
**Table:** Thermodynamics of aggregation into solid phase (model)

	Hydrophobic	Electrostatic	
$\Delta_b G$ (kJ/mol)	-67	+29	(0.33 mM)
$\Delta_b H$ (kJ/mol)	-106	-7	(any conc.)
$T\Delta_b S$ (kJ/mol)	-39	-36	(0.33 mM)

# Packing model

Packing diagram of dodecylamine complex with dodecyl sulfate

- Crystallographic data of most similar O-lauroylethanolamine – dodecylsulfate structure was used\*.
- O-lauroylethanolamine was substituted with dodecylamine.
- Resulting structure was optimized using the semiempirical quantum chemistry program MOPAC.



\*Tarafdar et al. *J. Phys. Chem. B* **114** (2010) 13710

- Association and aggregation reactions between long-chain aliphatic surfactants at temperatures below the fusion temperature are enthalpy-driven and entropy-opposed.
- The dominating enthalpy contribution is primarily due to aliphatic chain packing.

# Acknowledgment



## Project collaborators:

Daumantas Matulis,  
Povilas Norvaišas

## Financial support:

Research Council of  
Lithuania



# Appendix

# Dodecylammonium binding to decane sulfonate

ITC fitting parameters at three different concentrations in the cell

**Table:** Binding constants  $K_b^{fit}$  obtained from experimental data fits are compared to binding constants  $K_b^{mod}$  obtained from the model

$C$ (mM)	$\Delta H^{obs}$ (kJ/mol)	$N^{obs}$	$K_b^{obs}$ ( $M^{-1}$ )	$K_b^{mod}$ ( $M^{-1}$ )
0.66	$-70.9 \pm 3.7$	$1.01 \pm 0.03$	$(3.5 \pm 0.4) \times 10^5$	$5.5 \times 10^5$
0.33	$-70.5 \pm 5.2$	$0.98 \pm 0.05$	$(1.9 \pm 0.4) \times 10^5$	$2.4 \times 10^5$
0.165	$-72.7 \pm 15.9$	$0.99 \pm 0.03$	$(1.1 \pm 0.3) \times 10^5$	$1.4 \times 10^5$

# Thermodynamic parameters of coprecipitate formation

Alkane sulfonate binding to alkylammonium at 25°C

<i>m</i>	$K_b^{obs}$ (M <sup>-1</sup> )	$K_b^{mod}$ (M <sup>-1</sup> )	$\Delta_{agg}G$ (kJ/mol)			$\Delta_{agg}H$ (kJ/mol)			$T\Delta_{agg}S$ (kJ/mol)
			<i>obs</i>	<i>mod</i>	<i>alk</i>	<i>obs</i>	<i>mod</i>	<i>alk</i>	
21	$3.3 \times 10^4$	$6.4 \times 10^4$	-25.8	-27.5	-56.0	-37.4	-97.4	-90.8	-11.6
22	$1.8 \times 10^5$	$2.7 \times 10^5$	-30.0	-31.0	-59.6	-67.5	-102.6	-96.0	-37.4
23	$2.6 \times 10^5$	$1.2 \times 10^6$	-30.9	-34.6	-63.2	-81.9	-107.8	-101.2	-51.0
24	$1.3 \times 10^6$	$4.9 \times 10^6$	-34.9	-38.2	-66.8	-91.1	-113.0	-106.4	-56.3

$$\Delta_{agg} G^{mod} = \Delta_{agg} G_{ion} + \Delta_{agg} G_{alk} \quad (1)$$

$$\Delta_{agg} G_{ion} = -RT \ln(A_{ion} C) \quad (2)$$

$$\Delta_{agg} G_{alk} = -RT \ln(A_{alk} C) = -RT(m \ln(\Delta w) + \ln(w_0) + \ln(C)) \quad (3)$$

$C$  – molar concentration of detergent.

$$A_{ion} = B^{-1} \frac{[R_1 NH_3^+ \cdots R_2 SO_3^-]}{[R_1 NH_3^+][R_2 SO_3^-]} \quad (4)$$

$$A_{alk} = C^{-1} \frac{[R_1 NH_3^+ \cdots R_2 SO_3^- \downarrow]}{[R_1 NH_3^+ \cdots R_2 SO_3^-]} \quad (5)$$

$$K_b^{mod} = \frac{[R_1 NH_3^+ \cdots R_2 SO_3^- \downarrow]}{[R_1 NH_3^+][R_2 SO_3^-]} = A_{ion} B A_{alk} C \quad (6)$$

$B$  – constant factor equal to  $4.03 \times 10^{-5}$ .